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THE ACCESS MECHANISM

FOR THE 350

RANDOM **.ACCESS** MEMORY

by

W. E. DICKINSON February **24, 1956**

ABSTRACT

\ --.* .. --- ? ! **This report is about** the **access** mechanism **of** the **350** ' ' Random **Access** Memory. The **general arrangement and** the **details of** the electrical control circuitry **are** ¹**covered.**

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Introduction

Probably **the** one .portion of the 350, Random-Access **Memory, about which** more concern has **been** expressed and toward **which** most **inquiries have** been directed is the access mechanism **which** positions the magnetic **heads** to the information **tracks.** report **has been** prepared.to **help clarify this** situation.

Because feedback-control systems may be unfamiliar to some, the system is presented **first** in a general fashion **and** is then followed by a **detailed** account of **several** aspects of **the system.**

Since the access time is of **such** fundamental **importance** in **any** memory **device,** one of **the aspects** treated **in detail** is **the** fundamental **speed** limitations of **the** access mechapism and control **system** used. **In** addition, **details** of **relay circuitry** and of **the** control-system dynamics are discussed.

M,ore detail is **included** than.is generally desired in **order** to provide information **specific** interests.

Phvsical Arrangement

The basic **function** of the **access mechanism** bf the. **350** is to postion a pair **of** magnetic **heads** to **any** track on **any disk** of therandom-access **machine.** The fifty recording **disks** are stacked on a vertical **axis. The** magnetic heads **are** mounted in a pair of **arms which have** radial freedom.

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To position **the heads** to **any** track on **the disk** array, two drive motione **are used, Positioning** to the **deaired disk** is accomplished with a vertical drive, and to the deaired track with a **radial** drive. Figure 1 illustrates the **mechanical** portion of **the** acceas **mechanism,**

The arms are guided, for **radial** motion, in **bearings** on the carriage. Within **these bearings** the **arms are** capable of about **six** inches of **radial** motion. The inner five inches position the heads over **the** disk recording area. When **the arms are** in their **outermost** position, the **arm% are** completely outside of the **disks. This** is the position the arms **are** in during vertical-drive motion.

The carriage, during vertical m~tion, slides on a vertical 'way'. **At** eachof the fifty disk positions a detent **hole** is provided in the way. **A** pneumatic-detent piston is energized upon arrival at the desired disk. This detent, by means of a mechanical linkage, controls an interlock which frees the carriage and locks the arms for vertical drive, and **frees** the arms **and** locks the carriage for **radial** drive. The arms are capable of being freed only when the carriage is positioned properly at a **disk** and the **carriage** is capable of **being** freed **only** when the arms **are** completely outside of **the** dieks. Thus, a safe interlock **is** provided to prevent mechanical **damage** to the disk **assembly.**

The driving force is provided by a pair of magnetic -oowder, motor -driven, counter-rotating clutches. These clutches have a common-ouput shaft on which is located a drive caostan. **A small,** ateel **cable** connects the drive capatan to the arms through a system of three **pulleys. When** the arms are locked the carriage ia **free** and clutch torques result in vertical-drive motion.

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Similarly, when the carriage is detented the arms are free and the same clutches control radial motion. **In addition** to **the** detent **for** locking **the carriage,** a **detent** is provided to **position the arma to** their final **accuracy. This** feature greatly relieves the positioning requirements of **the** position-feedback **controller.**

The clutches **are** controlled by a **feedback-control system. Position** signals **for the** radial **and the** vertical **drives are obtained** from potentiometers on **the carriage and** on **the** way, respectively. **For stabilization** of **the feedback** loop a velocity **signal is** obtained from **a** tachometer **located** on **the** clutch-output **shaft. A** d-c control **system** is **used. The use** of relatively large voltages on **the potentiometers essentially** eliminates **any** drift **problems.**

Hereafter, **the** radial drive will be referred to **as** the track drive **as** it **is associated** with selection of a track, and **the** vertical **drive** will be **referred** to as the **disk drive.**

Electrical **Control System**

The control system **energizes** the two **clutches** so as to properly position the **arms.** The basic system used for track drive and for disk drive is the same. However, **because** the **distance** between **disks** is greater **than the distance** between tracks, and **because the** masses of **the arm and of** the **carriage are** different, the dynamics of the two **drives differ.**

To explaFn **the operation of the** control **system the** disk **drive will be** used.

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The **disk-drive** potentiometer **is** a linear-motion potentiometer. The resistance element is **attached** to **the frame;** the vdper is attached to **the carriage.** Fifty taps **are equally** spaced dong **the** resistance **element** such that when the wiper is adjacent to a tap it is positioned to a corresponding disk. **A reference-voltage supply, which** is electrically floating, establishes a voltage gradient along this resistance element. One of the fifty taps is electrically grounded through the disk-addressrelay pointa. When the wiper is **above** this tap it sees a positive **voltage,** when below, a negative voltage. **This** voltage is fed **into** the control amplifier **which,** in turn, energizes the appropriate clutch to **drive** the wiper toward **zero** voltage. ~ecause of the kinetic anergy stored **in** the moving carriage, it **is** necessary to anticipate arrival at the correct disk so the stopping clutch **can** be energized early enough' to **prevent** significant over shoot. This anticipation is provided by **the** tachometer **voltage. The** tachometer voltage is subtracted **from** the potentiometer voltage. Thus, when the carriage is moving toward the correct disk a voltage reversal is accomplished prior to the arrival. This energizes the stopping clutch. As the stopping clutch is energized, the **carriage** slows **down** decreasing the tachometer voltage, concurrently, **the** potentiometer voltage is decreasing toward zero. With proper adjustment, the carriage can be made to come to a stop **nearly** simultaneously with the potentiometer voltage reaching zero.

To position the **arms** to a **new address** a few logical choices must be **made.** If the **new** address is on the **same disk** it **is only necessary** to **radially drive the** arms to their **outermost** position, switch to disk **drive,** go to the **correct disk,** then **drive radially again** to **the** correct track.

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The remainder of this report will **cover in much greater detail the speed Um**itations, the relay-addressing system, the control-system logic and the feed**back-control-system dynamics.**

Access Time Considerations

The limitations on the speed of access will **be considered in this section. 'Since the various system parameters enter into the access time, numerical values** \. will be substituted after some preliminary equations and ideas are developed.

The basic system consists of a drive shaft ,on which is mounted the output members of both **magnetic clutches, the tachometer rotor, and the drive capstan, The drive capstan, in turn, is coupled to the carriage (for vertical motion) and to the arms (for radial motion) by means of a flexible-steel cable.** The **radius of** the **drive capstan determines the relative velocity of the drive shaft to the carriage (or the arms). ^I**

The inertia of the system referred to the drive shaft is:

 $J = J_d + R^2 M$

where,

 \equiv **inertia of drive shaft R** = **radius of** the **capstan** $M =$ mass of driven member

The optimum capstan radius can-be determined by finding the radius which causes the driven member **to move the furthest** for **a given torque in a given** time..

 (1)

The driven abaft turna through an angle. 0

$$
\Theta = \frac{T t^2}{2 (J d + R^2 M)}
$$

where,

T is torque applied to drive shaft

t is time

The driven member travels a distance, x = **RO or:**

$$
X = \frac{R T t^2}{2 (J_d + R^2 M)}
$$
 (3)

Maximizing x with respect to R:

$$
\frac{dx}{d R} = 0 = \frac{2 (J_d + R^2 M) T t^2 - 4 R^2 M T t^2}{4 (J_d + R^2 M)^2}
$$

$$
J_d = R^2 M
$$

Thue, the radius. should be chosen to make the two inertias equal. It **can be shown that this same radius is also optimum for the case where the driven** member accelerates to its terminal velocity, runs at constant speed and then , . **decelerates to a stop.**

The mass for disk drive is about three times the mass for track drive. There**fore, the capetan radius should be about seventy per cent larger for the track drive. A compromise radlue must be chosen. Fortunately, the optimum is a broad one, but this analysie does point out that an improvement in access speed** 1 **cannot be obtained by going to a larger capetan.**

 (2)

 $\langle 4 \rangle$

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The clutch-input members are driven by a motor at nearly constant speed. **if a clutch ie engaged long enough to bring its output member up to this rotational speed, the drive cable moves at about 100 inches per second. Whether the cable gete to this terminal velocity or not depends upon the torque available., and the disbnce the driven** member **is to move.**

To simplify the calculations somewhat all parameters now will be referred to the **driven member. The idealized conditions given here** will **permit evaluation of the maximum access speed8 possible with this access aystem.**

When 'the available force ia insufficient to get the mass up to the terminal velocity, acceleration must take place for one-half the travel distance and deceleration for the other half. For this case the' travel tima is exprea sed aa:

$$
t = 2 \sqrt{\frac{S M}{F}}
$$

Where, S = **distance to be travelled,** M = **mass referred to the driven member, including driveshaft inertia. .F** = **available driving force.**

When the available force is sufficient to get the mass up to the terminal velocity **in,less than one-half the travel distance, a** portion **of** *the* **travel can be accomplished at the terminal velocity. For this case the time to accelerate is:**

$$
\frac{V}{A} = \frac{VM}{F}
$$

where, V = **terminal velocity A** = **acceleration**

 (6)

 $\pmb{\mathsf{t}}$

 (5)

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(7)

 (8)

 (9)

The same time is requiradto decelerate. The average velocity during these times will be $\frac{V}{2}$ **thus, the time-for the distance travelled at full speed will be:**
 $\frac{S}{V}$ - $\frac{VM}{F}$ **2**

The total time **to trayel the distance S'on disk or track drive is:,**

$$
t = S + VM
$$

To travel from one disk to another:

$$
t = \frac{S}{V} + \frac{3VM}{F}
$$

When a terminal velocity of 100 inchea per eecond is used with our present clutchae, equation 8 holds for the **maximum travel case, i. e. inner track on lowest disk to inner track on highest disk. '(32 inches) Substituting numbers into equation 8 yie1ds.a drive time of:**

$$
t = 0.32 + \frac{2.73}{F}
$$

where, F is the drive force in pounds and.must be greater than 15 for this expre asion to be valid

 $M = 3.5$ pounds is used.

This gives times from **.374 second3 to .502 seconds for forcea of 50 and 15** pounds, respectively.

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 $\frac{1}{2}$

To **these** idealized **times** rnustbe **added other** time **required** in **the** system. **Due** to **the inductance** in the clutch coil about **.020** seconds is **required** to de**velop the** output torque. Although, **the same delay can** be **anticipated** in stopping, the control problem is more **difficult** and at least **the same time** need be **added** for stopping on **each** of the **three drive** motions. (On starting, a clutch is turned full on whereas on stopping, both **clutches** are **called** upon to **cause** the **driven** member to follow a **certain** position-velocity trajectory) **This** delay adds. 120 seconds to the drive time. Upon completion of the disk drive a mechanical detent is **engaged,** this takes **about** 0.025 **seconds.** Upon arrival at **the** correct track a **track** detent **is engaged** and the **heads are brought** to the **disk surface. The** time **required** for this, **plus** a **safety-factor delay, requires** about 0.080 seconds.

Totaling these times **gives** an **access** time **ranging from .600** to .720 seconda **being** possible, with the **ranges** of **drive** force given **above,** for **traveling** to the inner **track** on the bottom **disk** from **the her** track on **the** top disk or **vice versa. The** power limitations come into **the picture** when the **terminal velocity** is **increased significantly.** In **starting,** the accelerating-clutch **slip-** speed **goea** :from **100** radians per second **to** zero; **whereas, the** stopping-clutch slip **speed goes** from 200 radians per second to 100 radians per second when the cable velocity
 100 inches per second. At 50 inch-pounds torque the energy required is:
 50 in - 1b x 50 $\frac{rad}{sec} \times \frac{91}{50}$ **sec** = 45.5 in - 1b starting **is 100 inches** per **second.** At 50 **inch-pounds torque** the **energy required** is:

sec 50 50 in - 1b x $\frac{50 \text{ rad}}{\text{sec}} \times \frac{91}{50}$ sec = 45.5 in - 1b starting

50 in - 1b x 150 rad x $\frac{91}{\text{sec}}$ sec = 136.5 in - 1b stopping $50 \text{ in } -10 \times 150 \text{ rad } \times .91$
 $\frac{91}{\text{sec}}$ (45.5 + 136.5) **3** = 546 in - **lb** energy of **access** lost in clutches

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due to accelerating and **decelerating. About 100** in-lb **of energy must be added** for **frictional losses.** For **0.600 second access time this gives an average-power dissipation of 0.163 horsepower during access. If the terminal velocity is** doubled the energy of accelerating and decelerating quadruples. The potential **access time drops to about 0.49 second, whereas, the average-power dissipated** during access rises to 0.71 horsepower. The average-power dissipated during 1 - shorter **accesses is even greater, since the power is lost** during **accelerating'** 1 **and decelerating periods. If** the **duty cycle of** the **acceaa mechanism is low enough,** these **access times** are **possible since** the **average power drops. However, clutch life under these stringent conditions did** not **look promising and** compli**cations in** driving **the clutches with the drive** motor **made' selection** of **our** present drive **speed more** desirable.

The **acces s times developed** in **this section are** based upon proper **adjustment. The** significance of **these adjustments** will **be developed** in **the section** dealing **with the** dynamics **of** the control **aystem.**

he **I2e'lay Addressing** System

5 7'

In both the **disk** and the track-addressing systems the method chosen permits **the potentiometers** used to **have** a **lower** linearity requirement than **is** required **with untappe** d-potentiometer **systems.**

The disk potentiometer is **made of-a** conductive-plaatic strip which **has** fifty **taps, one for each** disk. The **strip has its two end** terminals **connected** to an electri-, **ally-floating d-c voltage** source. **One** of **the** fifty **taps** is **grounded through** the

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points of the addres s relays. A wiper moves along this strip and is the PO sitionkg sip1 for disk drive. See Figure 2. When not at the **grounded tap a voltage of about 2.5 volts per disk error is obtained.** The **exact voltage between taps is** not **critical since zero voltage is obtained at the desired disk by virtue of a pre cisely located tap. A moderate** linearity **of about five per** cent **is desirable from** the control standpoint.

 ~ 0.1

 $\label{eq:2.1} \mathcal{L}(\mathcal{L}) = \mathcal{L}(\mathcal{L})$

 $\mathcal{L}^{(1)}_{\text{max}}(\mathbf{z})$

 $\sim 10^{11}$

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DISK ADDRESS SYSTEM

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 $\mathcal{L}_{\mathcal{A}}$

 $\begin{picture}(180,10) \put(0,0){\line(1,0){10}} \put(10,0){\line(1,0){10}} \put(10,0){\line($

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The track potentiometer is arranged in a similar manner but it is not feasible, nor **necessary, to have** one-hundred **taps to correspond to** each of **the** track . . locations. **Here instead, six taps** are provided with **the section between adjacent** taps **corresponding** to twenty **track positions. To select** indfvidual **tracks. twenty equal, fired resistors, in series, are connected acrosa** a pair of adjacent **taps. The null position on** the potentiometer **ia shifted along by** grounding **at** one point **along** the **twenty resistor chain. See Figure 3. This arrangement requires the** potentiometer to **have** sufficient **linearity between taps** to indicate **the position adequately, but relieves** the **overall** linearity requirement **by a** factor **of** *sic* from an untapped-potentiometer syatem. The **gradient along this** track potentiometer is **about 1.2** volta per **track.**

In addition to **the one-hundred** track **addresses** there **is one other address** required on **track** drive. **This is** the **position where** the **arm** is **fully** retracted for travelling **between diska called the** "homel'.address. **This position is** established by a **potentiometer connected** between the tap corresponding to the outermost **track** and **the end** terminal of **the** potentiometer. **See** Figure **3. The** track addresa or the "home" **addres B ia chosen** by a transfer **point** on **'a relay which grounds** either a point **along the** twenty-resistor **chain** or the wiper of **the** aforementioned potentiometei,

Control -System **Logic**

The control-system logic **consists** of a group of relays **which,** based on certain **inputs,** decide **what actions** need **to** be **taken** to position **the heads** to the selected **address,**

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The general procedure followed was to set up all possible combinations of the input conditions, rule out all those which are mechanically prevented and define **the actions to be taken for the remaining combinations.** -

The **input conditions used are as follows:**

- I **A. Start signal from controlling source.**
	- **B. Disk** detent **engaged. (Arm free, carriage locked)**
- **C.** Disk detent disengaged. (Carriage free, arm locked in. **home** position) ,
- D. Disk null.
- E. Track null.
- **F. Clutch power.**

,Both **conditions of the disk detent are included since, although they are mutually** . .. **exclusive, the disk detent may be between the two conditions.**

The controlled **relays** are **liated** below:

- , **A. Start relay**
- **B. Disk-drive relay (negative** = track **drive).**
- . **C. Track-address** relay **(negative** = home **address).**
- D. Clutch-power **relay.**
- E. **Disk detent.**
- **F. Arrival sequence.**

The start relay **is a** key relay **in the system.** The **disk-drive relay feeds the** disk-positicn **or** the track-po sition error **to** the control amplifier ; **when disk** driving **the** reiay **is** picked,' **when** track driving the relay **ia dropped.** The **trackaddress** relay **s** witches between the **selected** track **address or** the home -position

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address. The **clutch-power relay interrupts power to** the **clutches.** The disk detent **is** engaged by **energizing** a solenoid **valve, the detent itself is.** pneumatic. **The arrival sequence consists of removing clutch** power, **track detenting,** putt- .ing the mapretic **heads on the disk and after a suitable delay giving** the **ready signal to** the **machine using** the **350.**

The possible combinations **of** inputs **and** the **action taken by the controlled relays** will be **listed** separately on Figure 4 .

The following listing **give** s conditions for **a normal-acces s sequence.** The actions **to** be **taken are** listed **for each condition. These are the basis** for **the** logic **used** . in the control **system.**

1. Awaiting next command, **start signal off.**

Ready for **track drive. Disk** detent **engaged. Clutch** power off. **Track detent** de **-energized.**

2. **New address put** into **address relays.**

Home **address chosen** if **new disk,** if **not, track address is chosen.**

e

3. Start **signal** given **(assume** new disk **addressed).**

Start relay **picked.** Disk detent de **-energized.** Clutch power on.

4. Arrival **at** home position and **&sk** detent begins to disengage.

Clutch power off.

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5. Disk detent disengaged

Disk drive chosen. Clutch power on.

6. Arrival at correct disk

Track address chosen. Disk detent energized. Clutch power off.

7. Disk detent starts to engage

Track drive chosen.

8. Disk detent engaged

Clutch power on.

9. Arrival at the correct track

Arrival sequence.

 $\label{eq:2.1} \mathcal{L}(\mathcal{L}) = \mathcal{L}(\mathcal{L}) \left(\mathcal{L}(\mathcal{L}) \right) \left(\mathcal{L}(\mathcal{L}) \right) \left(\mathcal{L}(\mathcal{L}) \right)$

 $\label{eq:2} \frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1$

In addition to the normal sequence, provisions must be made to handle abnormal input combinations so as to route them into the normal sequence given above.

 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2.$

 $\label{eq:2.1} \mathcal{L}(\mathcal{L}(\mathcal{L})) = \mathcal{L}(\mathcal{L}(\mathcal{L})) = \mathcal{L}(\mathcal{L}(\mathcal{L}))$

These are indicated in Figure 4.

 $\label{eq:2.1} \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}})) \leq \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}})) \leq \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}))$

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CONTROL - SYSTEM LOGIC

 $\mathcal{L}^{\text{max}}_{\text{max}}$

SYMBOLS 1 - OPERATE 0 - DON'T OPERATE x - DON T CARE

 $\label{eq:2} \frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^{2} \left(\frac{1}{\sqrt{2}}\right)^{2} \left(\frac{$

 $\label{eq:2.1} \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}})) \leq \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}})) \leq \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}))$

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Control - **System Dynamics**

A rigorous analysis of the control-system dynamics will **not be made because nearly every component in the feedback loop has some non-linearity and at least, one** nonlinear **element has been added.' However, an approximate** linear **analysis givaa some insight into the dynamic behavior. A description of the uae of positionerror** limiting **shows how differences** in **clutch characteriatics can be compensated.**

The linear **analysis will use root-locus techniques.** * **The block diagram below** represents the feedback-control system over the frequency range of inferest.

Each of these blocks -will **be discuseed before** contindng **with the analysis.** The **letter "ptl in each block represents the complex-frequency variable, w** + j w.

The **amplifier** block **has a non-frequency-sensitive term,** Kl, **which is** the d-c **voltage** gain **of** the amplifier. **The value of K1 depends upon the size of the error** voltage, but it is about 400 near zero input. The two time-constants, T1 and T2, **represent** the **effect of an** R-C network **in** the **amplifier.**

The constant, K2, represents the torque-to-current ratio for the clutch, which for the coil we use is about 400 inch-pounds per ampere. $R + L_p$ represents the impedance **of** the coil.

* See Control-System Dynamics by W. R. Evans, McGraw-Hill, 1954

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This block has voltage input and torque output

The inertia term is made up of the inertia of the load and of the 'clutch-output shaft. It **has a value near 3.5 pound-inch. A viacous -damping (resisting torque proportional to angular velocity) term is added. representing the torque to velocity ratio. A value I of 0.27 inch-pound-second per radian ia uaed for B. This block has torque input and angle output.**

The tachometer and potentiometer. terms are adjustable and differ for track and diak drives. Kj has a maximum value of *0.36* **volt-sec per radian and Kq has 25 volta per.** radian for track and 7.5 volts per radian for disk drive. This block converts angle to **voltage.**

The closed-loop transfer function is expressed as:

$$
\frac{C}{R} (p) = \frac{K_1 K_2 (p + T_1)}{L J p (p + \frac{1}{T}) (p + \frac{1}{T}) (p + \frac{1}{T}) K_1 K_2 K_3 (p + \frac{1}{T})} = \frac{1}{T_3}
$$

Where time -constant substitutions have been made as follows:

- T_3 represents the ratio K_3/K_4
- **T4 represents the ratio L/R**
- **T5 represents the ratio** J/B

The **zero of equation 10 occurs when p** = **-1** . **To** findthe **poles. root~locua** - **Ti**
T 1 **1 techniques** will **be uaed. The** denominator **is rewritten in a suitable** form **for root-locus analysis.**

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$$
D = K_1 K_2 K_3 (p + T_1 (p + T_3) \left[L_J p (p + T_2) (p + T_3) (p + T_3) + 1 \right] \qquad (11)
$$

The **complex-frequencies, p, which make the bracketted term zero, are** the **poles of equation 10. (At these frequencies, an output is obtained for zero input.**) Lumping all the non-frequency-sensitive terms into $M = LJ/K_1-K_2-K_3$ and re**writing the bracketted** term **only.** . . .

$$
Y = M p (p + \frac{1}{T}z(p + \frac{1}{T}) + 1)
$$
\n
$$
(p + \frac{1}{T}p + \frac{1}{T}z)
$$
\n(12)

 \mathbf{or}

$$
\frac{MP (p + \frac{1}{12}(p + \frac{1}{14}p + \frac{1}{13})}{(p + \frac{1}{11}(p + \frac{1}{13})}) = |1| \frac{\sqrt{80^{\circ}}}{180^{\circ}}
$$
 (13)

As M varies from' zero to infinity **a locus of roots, (value8 of p) which eatiafy equation** 13. can be traced on the p-plane. The root-locus technique solves (13) by finding the **values of** p **which satiefy the** angle **criterion first,** then **values of p on these loci which satisfy the gain term, M. Because T3 can be set'at a range of values the effect of various varying Tg** will **be ahown by a eeriea of root -locue sketches, aee Figures 5,** *6* **and 7.**

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 $\bar{ }$

FIGURE

 $\frac{1}{2} \sum_{i=1}^{2} \frac{1}{2} \sum_{j=1}^{2} \frac{1}{2} \sum_{j=1}^{2$

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In these plots $1/T_3$ is assigned values of -40, -30 and -20. For these values one real pole of the closed-loop transfer function varies from -59 to -53 , the other real pole stays with $-1/T_3$ going from -39 to -19. The complex poles vary from a damping ratio of 0.37 to about 0.5 at a natural frequency of about 10 cycles per second. The significance of the location of poles and zeros is considered in the literature. The general expression for the time response of the above system to a step input can be expressed as:

 $C(t) = A_0 + A_1 \varepsilon^{-p} + A_z \varepsilon^{-p} + A_3 \varepsilon^{-p}$ sin (w t + ϕ) (14)

The responses for the three pole-and-zero configurations are shown in the accompanying time-response curves on Figures 5, 6 and 7. These curves obviously hold only for the short travel where the overall system is linear.

Because of the way this controller operates it is very similar to the operation of an "on-off" controller. (The only difference is that here the controller has a proportional region to operate in for small error signals.) With this type of controller it is necessary to determine the switching time.* Because the plot of error versus error rate is nearly a parabola, an attempt was made to achieve this curve in this controller by use of a controlled limiter. This limiter distorts the error voltage versus error curve so as to approximate the parabolic-switching curve. By using separate limiter controls for the two polarities of position error, an independent adjustment is provided to compensate for the differences between magnetic clutches. This adjustment is provided as a means of obtaining the desired performance and yet to allow a wide tolerance in the clutch, torque-current characteristics.

A very applicable article is: "Some Design Considerations of a Saturating \ast Servomechanism." by P. E. Kendall and J. F. Marquardt Proc. Nat'l. Elec. Conference Vol. IX. Stant